

Cluster-tilted algebras as trivial extensions

Thomas Brüstle (Sherbrooke)

Given an algebra C of global dimension at most two, we study the trivial extension $\tilde{C} = C \ltimes \text{Ext}^2(DC, C)$ of C by the $C - C$ -bimodule $\text{Ext}^2(DC, C)$. If the algebra C is tilted, then the extension \tilde{C} is cluster-tilted, and every cluster-tilted algebra arises in this way. The aim of the lecture is to study various properties of the construction $C \mapsto \tilde{C}$. For instance, the quiver of the trivial extension \tilde{C} is easily obtained from the quiver of C by adding an arrow in the reverse direction wherever there is a relation in C . This is based on joint work with Ibrahim Assem and Ralf Schiffler.